

to measure the value of science by the number of dollars- he thinks it is likely to bring into his pocket, and if he does not see the dollars, he is very disinclined to disturb his ancient prejudices. **But only give him plenty of rope, and when the new views have become fashionably current, he may~ find it worth his while to adopt them, though, perhaps, in a somewhat sneaking manner,** not unmixed with bluster, and make believe he knew all about it when he was a little boy. He sees a prospect of dollars in the distance, that is the-

338 ELECTROMAGNETIC THEORY. CH. IV.

reason. The perfect obstruction having failed, try the perfect conduction.

You should make your converts out of the rising generation and the coming men. Thus, passing to another matter, Prof. Tait says he cannot understand my vectors, though he can understand much harder things. But men who have no quaternionic prejudices can understand them, and do. Younger men are born into the world with more advanced ideas, on the average. There cannot be a doubt about it. If you had taught the Calculus to the ancient Britons you would not have found a man to take it in amongst the whole lot, Druids and all. Consider too, what a trouble scientific men used to have with the principle of the persistence of energy. They could not see it. But everybody sees it now. The important thing is to begin early, and train up the young stick as you want it to grow. Now with Quaternions it is different. You may put off till to-morrow what you cannot do to-day, for fear you commence the study too soon. Of course, I" refer to the Hamilton-Tait system, where you have to do violence to reason by making believe that a vector is a quaternion, and that its square is negative.

According to Ohm's law alone, a perfect conductor should be one which carried an infinite current under a finite voltage, and the current would flow all through it because it does so ordinarily. But what is left out of consideration here is the

manner in which the assumed steady state is established. If we take this into account, we find that there is no steady state when the resistance is zero, for the variable period is infinitely prolonged, and Ohm's law is therefore out of it, so far as the usual application goes. In a circuit of no resistance containing a finite steady impressed voltage E , the current would mount up infinitely and never stop mounting up. On the other hand, if we insert a resistance R in the former circuit of no resistance, there will be a settling to a steady state, for the current in the circuit will tend to the value E/R , in full obedience to Ohm's law. The current is the same all round the circuit, although a part thereof has no resistance. We conclude that that portion has also no voltage.

But this is only a part of the story. Although we harmonise with Ohm's law, we overlook the most interesting part. The

THEORY OF PLANE ELECTROMAGNETIC WAVES. 339

smaller the resistance the greater the time taken for the current to get into the conductor from its boundary, where it is initiated. In the limit, with no resistance, it never gets in at all. Where, then, is the current? For, as we have said, it mounts up to a finite value if there be a finite resistance inserted along with the perfect conductor, and mounts up infinitely if there be no resistance.

We recognise the existence of electric current in a wire by the magnetic force round it, and in fact measure the current by its magnetic force. Therefore, according to this, there is the same total current in the wire, if the magnetic force outside it remains the same. If, then, the magnetic force stops completely at the surface of the wire, whose interior is entirely free from magnetic force, the measure of the current is just the same. The uniformly distributed current of the steady state appropriate to finite conductivity becomes a mere surface current when the conductivity is infinite. In one case we have a finite volume-density of current, and in the other a

finite surface-density. When the current inside the wire is zero so is the electric force, in accordance with Ohm's law again. The electric and magnetic phenomena are entirely in the dielectric outside the wire, the entrance of any similar manifestations into it being perfectly obstructed by the absence of resistance. For this purpose the thinnest skin would serve equally well. In the usual sense that an electric current is a phenomenon of matter, it has become quite an abstraction, for there is no matter concerned in it. It is shut out completely. In the circuit of finite resistance, a portion of which is a wire of no resistance, supporting a steady current, there is no difference whatever in the external, magnetic force outside the resisting and non-resisting parts, though in one case there is entrance of the magnetic force and waste of energy, whilst in the other there is no entrance and no waste. These conclusions do not rest upon Maxwell's theory of dielectrics, but upon the second circuital law of electromagnetism applied to conductors. But it is only by means of Maxwell's theory that we can come to a proper understanding and explanation of the functions of conductors.

The sense in which a perfect conductor is a perfect conductor in reality as well as in name is that it allows electro-

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310 ELECTROMAGNETIC THEORY CIL IV.

magnetic waves to slip along its surface in a perfectly free-manner, without waste of energy. Though perfectly obstructive internally, it is perfectly conductive superficially. It merely guides the waves, and in this less technical sense of conduction the idea of a perfect conductor acquires fresh life.

The Effect of a Perfect Conductor on External Disturbances. Reflection and Conduction of Waves.

190. The conditions at the interface of a perfect conductor

and a dielectric are that the electric force in the dielectric has no tangential component and the magnetic induction no normal component. Or

$$\nabla \cdot \mathbf{E} = 0, \quad \nabla \times \mathbf{H} = 0,$$

if \mathbf{N} be the unit normal from the conductor. Thus, when there is electric force at the boundary it is entirely normal, with electrification to match; and if there is magnetic force it is entirely tangential, with electric current to match. Both electrification and current are superficial. The displacement measures the surface density σ of the one, and the magnetic force that of the other, say c , thus

$$\sigma = \mathbf{N} \cdot \mathbf{D}, \quad c = \mathbf{N} \times \mathbf{H},$$

in rational units, without any useless and arbitrary 4π constant, such as is required in the B.A. system of units, of amazing irrationality. If, then, we have electromagnetic disturbances given in a dielectric containing a perfect conductor, the latter first of all is free from disturbance, and next causes such reflected waves as to annihilate the tangentiality of the electric force and the normality of the magnetic force.

As regards steady states, the influence of a perfect conductor on induction due to foreign sources is to exclude it in the same manner as if the inductivity were made zero; that is, the induction goes round it tangentially instead of entering it. This is usually ascribed to an electric current-sheet induced upon its surface, whose internal magnetic force is the negative of that due to the external field. This is right mathematically, but is deceptive and delusive physically. There is no internal force, neither that of the external field nor that of the superficial current. The current sheet itself merely means the abrupt

to be the source of magnetic force in a body which cannot permit its entrance. The previously mentioned case of a perfectly conducting wire inserted in a circuit of finite resistance supporting a steady current, will serve to bring out this point strongly. The supposed induced superficial current is now actually the main current in the circuit itself.

It is different with the steady state due to external electric sources. The displacement is just as much shut out from the perfect conductor (which may also be a dielectric) as was the magnetic induction, but in a strikingly different manner, terminating upon it perpendicularly, as if it entered it in the manner that would happen were the conductor nonconducting, but of exceedingly great permittivity, so that it drew in the tubes of displacement.

Although a perfect magnetic conductor is, in the absence of knowledge even of a finite degree of magnetic conductivity, a very far-fetched idea, yet it is useful in electromagnetic theory to contrast with the perfect electric conductor. A perfect magnetic conductor behaves towards displacement just as a perfect electric conductor does towards induction ; that is, the displacement goes round it tangentially. It also behaves towards induction as a perfect electric conductor does towards displacement ; that is, the induction meets it perpendicularly, as if it possessed exceedingly great inductivity, without magnetic conductivity. This magnetic conductor is also perfectly obstructive internally, and is a perfect reflector, though not quite in the same way as electric conductors. The tangential magnetic force and the normal electric force are zero.

As regards waves, there are two extreme ways in which a perfect conductor behaves that is, extreme forms of the general behaviour. It may wholly conduct them, or it may wholly reflect them. In the latter case we may illustrate by imagining a thin plane electromagnetic sheet, consisting of crossed electric and magnetic forces in the ratio given by $E = vH$, moving at the speed of light, to strike a perfect conductor flush that is, all over at the same time, by reason of parallelism of the sheet and conducting surface. The incident sheet

is at once turned into another plane sheet, which runs away from the conductor as fast as it came. If the conductivity be

342 ELECTROMAGNETIC THEORY. OIL IV.

of the electric kind the reflected sheet differs from the incident in having its displacement reversed, but in no other respect* This is perfect reflection with reversal of E. During the act of reflection, whilst the incident and reflected sheets partly coincide, E is zero and H is doubled. Both are tangential ; but there can be no tangential E, so the reflector destroys E and initiates the reflected sheet, in which H is the same as in the incident sheet, whilst E is reversed.

On the other hand, when the conductivity is of the magnetic kind, the reflected wave sheet differs from the incident only in having its induction reversed. The displacement persists, being doubled during the act of reflection, whilst the induction is then annulled.

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https://en.wikipedia.org/wiki/Archibald_Howie

re cattq, <http://www.ivorcatt.co.uk/cattq.htm>, Howie is a westerner. Pepper, who reported to him as head of the Cavendish, is a southerner. (Both at Trinity.) They refuse to discuss their disagreement with each other or with us..

<http://www.ivorcatt.co.uk/x67d.htm>

Re: em

Inbox

29.3.2019

Prof. A Howie

to me

10:08 AM (8 hours ago)

Dear Ivor,

Thanks for our message. I admire your tenacity over EM theory which I'm sure keeps your brain firing away. I have never met Alex Yakovlev and had not even heard of him until maybe 6 months ago I came across his Phil Trans paper with its fulsome references to the work of you and your colleagues. Following our strenuous but unsuccessful efforts many years ago to resolve the difference between us, I am however not at all attracted by the idea of revisiting them!

In the past few months the "standard" EM theory that you dislike **[no; I want to be told what it is! See cattq.]** I have been applying to compute the energy loss experienced by a fast electron beam. This travels in the z direction and is highly focused to about 0.2nm in the x-y plane, when it passes just outside a dielectric material. This theory gives a very good account of many experimental observations. Of course by some amazing fluke it may still succeed when built on a foundation **[Howie's or Pepper's?]** that you believe to be incorrect but so far I am not convinced. **[Why does he not discuss his disagreement with Pepper on fundamentals - cattq? – IC]**

You may recall that long ago I encouraged you to get your ideas published in Physics Education in the guise of a challenge to the teaching of EM. I shared some of your disappointment and frustration when, after accepting it, they pulled out from publication. At least Yakovlev has now managed to get some account of your theory published in the scientific literature and we can await reactions. I am not too confident that much will emerge however since the serious readership of most published papers is now close to zero. Most papers are now read by bots as I discovered when a paper I recently submitted to Ultramicroscopy was accepted. Within a few hours (while it was still listed as an on-line paper in the publication pipeline) I got first an email from some organisation telling me that a number of people had already consulted my paper and that I could find out who they were by signing up with them. Hard on the heels of this came a second message offering for sale a mug on which the first page of my paper would be printed!

Best wishes,

Archie.

“Physics Education I shared some of your disappointment and frustration when, after accepting it, they pulled out from publication.” – AH
A few decades later the journal published an attack on me and the editor refused to let me reply.
“Physics Education”, a journal of the Institute of Physics.
<http://www.ivorcatt.co.uk/x311a.htm>

On 2019-03-28 21:11, Ivor Catt wrote:

> Dear Archie,
> I would greatly value your comment on
> [HTTP://WWW.IVORCATT.CO.UK/YAK7.HTM](http://www.ivorcatt.co.uk/yak7.htm) [1]
> Ivor
>
> Links:
> -----
> [1] <http://www.ivorcatt.co.uk/yak7.htm>