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A Treatise on Electricity and Magnetism VOLUME ONE

James Clerk Maxwell

A TREATISE ON

ELECTRICITY AND MAGNETISM

Ву

JAMES CLERK MAXWELL

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tung in die Elektrostatik, &c. I have confined myself almost entirely to the mathematical treatment of the subject, but I would recommend the student, after he has learned, experimentally if possible, what are the phenomena to be observed, to read carefully Faraday's Experimental Researches in Electricity. He will there find a strictly

at every instant as much must flow out of any given closed surface as flows into it.

It follows from this that every electric current must form a closed circuit. The importance of this result will be seen when we investigate the laws of electro-magnetism.

Since, as we have seen, the theory of direct action at a dis-

tance is mathematically identical with that of action by means of a medium, the actual phenomena may be explained by the one theory as well as by the other, provided suitable hypotheses be introduced when any difficulty occurs. Thus, Mossotti has de-

SPHERICAL HARMONICS. we find

 $+x^7y^6$ [18+ 90 y^2 +288 y^4 +735 y^6 +&c.]

 $+x^9y^6[32+200y^2+780y^4+&c.]$

 $+x^{11}y^{6}[50+375y^{2}+\&c.]$

 $+x^{8}y^{9}$ [32 + 192 y^{2} + &c.]

 $+x^{13}y^{6}[72+\&c.]$

 $+x^{10}y^{9}$ [144 + &c.]

 $q_1 = x^2$

 $p_1 = x^2 y^3 \begin{bmatrix} 2 + 3y^2 + 4y^4 + 5y^6 + 6y^8 + 7y^{10} + 8y^{12} + 9z^{-14} \end{bmatrix}$ $+x^5y^6$ [8+ 30 y^2 + 75 y^4 +154 y^6 +280 y^8 +&c.]

 $+x^5y^3$ [4+9 y^2 + 16 y^4 + 25 y^6 + 36 y^8 + 49 y^{10} +64 y^{12} +52]

It will be more convenient in subsequent operations to write these coefficients in terms of a, b, and c, and to arrange the terms according to their dimensions in c. This will make it easier =

 $+ (8a^2b^{15} + 154a^5b^{12} + 288a^7b^{10} + 32a^8b^9 + 200a^9b^8 + 50a^{11}b^6)e^{-7}$

. -

 $+x^{7}y^{3}$ [$6+18y^{2}+40y^{4}+75y^{6}+126y^{8}+196y^{10}+&c.$]

 $+x^9y^3[8+30y^2+80y^4+175y^6+336y^8+&c.]$

 $+x^{11}y^{3}[10+45y^{2}+140y^{4}+350y^{6}+&c.]$

 $+x^8y^6$ [16+ 72 y^2 + 209 y^4 +488 y^6 +&c.]

differentiate with respect to c. We thus find

 $+(7a^2b^{13}+75a^5b^{10}+90a^7b^8+32a^9b^6)c^{-15}$

 $+(6a^2b^{11}+39a^5b^8+18a^7b^6)c^{-13}$

 $p_1 = 2 a^2 b^3 c^{-5} + 3 a^2 b^5 c^{-7} + 4 a^2 b^7 c^{-9} + (5 a^2 b^9 + 8 a^5 b^6) c^{-11}$

 $+x^{10}y^{6}$ 60 + 342 y^{2} + 1222 y^{4} + &c.

 $+x^{13}y^{3}[12+63y^{2}+224y^{4}+&c.]$

 $+x^{15}y^3[14+84y^2+&c.]$

 $+x^{12}y^{6}[150+1050y^{2}+\&c.]$

 $+x^{17}y^3[16+\&c.]$

 $+x^{14}y^{6}[308+&c.]$

 $+x^{11}y^{9}$ 64 + &c.

(26)

(27)

+
$$(9a^2b^{17} + 280a^5b^{14} + 735a^7b^{12} + 192a^8b^{11} + 780a^9b^{10} + 144a^{10}b^9 + 375a^{11}b^8 + 72a^{13}b^6)c^{-19} + \dots$$
 (22)

 $z_1 = a^2c^{-2} + 4a^5b^3c^{-8} + (6a^7b^3 + 9a^5b^5)c^{-10}$ $+(8a^9b^3+18a^7b^5+16a^5b^7)c^{-12}$ $+(10a^{11}b^3+30a^9b^5+16a^8b^6+40a^7b^7+25a^5b^9)c^{-14}$ $+(12a^{13}b^3+45a^{11}b^5+60a^{10}b^6+80a^9b^7$

 $+72a^{8}b^{8}+75a^{7}b^{9}+36a^{5}b^{11})c^{-16}$ $+(14a^{15}b^3+63a^{13}b^5+150a^{12}b^6+140a^{11}b^7+342a^{10}b^8$ $+175a^{9}b^{9}+209a^{8}b^{10}+126a^{7}b^{11}+49a^{5}b^{13})c^{-18}$ $+(16a^{17}b^3+84a^{15}b^5+308a^{14}b^6+224a^{13}b^7+1050a^{12}b^8$ $+414a^{11}b^9+1222a^{10}b^{10}+336a^9b^{11}+488a^8b^{12}+196a^7b^{13}$ $+64a^5b^{15}$) $c^{-20}+...$ (23) $\tau_z = 3a^3b^3c^{-6} + 6a^3b^5c^{-8} + 10a^3b^7c^{-10} + (12a^6b^6 + 15a^3b^9)c^{-12}$ $+(27a^8b^6+54a^6b^8+21a^3b^{11})c^{-14}$

 $+(48a^{10}b^6+162a^8b^8+158a^6b^{10}+28a^3b^{13})c^{-16}$ $+(75a^{12}b^6+360a^{10}b^8+48a^9b^9+606a^8b^{10}$ $+372 a^6 b^{12} + 36 a^3 b^{15}) c^{-18} + \dots$ (24) $c_{1} = a^{3}c^{-3} + 6a^{6}b^{3}c^{-9} + (9a^{8}b^{3} + 18a^{6}b^{5})c^{-11}$ $+(12a^{10}b^3+36a^8b^5+40a^6b^7)c^{-13}$ $+ \left(15 a^{12} b^{3} + 60 a^{10} b^{5} + 24 a^{9} b^{6} + 100 a^{8} b^{7} + 75 a^{6} b^{9}\right) c^{-15}$

 $+(18a^{14}b^3+90a^{12}b^5+90a^{11}b^6+200a^{10}b^7$ $+126a^9b^8+225a^8b^9+126a^6b^{11})c^{-17}$ $+(21a^{16}b^3+126a^{14}b^5+225a^{13}b^6+350a^{12}b^7+594a^{11}b^8$ $+525a^{10}b^9+418a^9b^{10}+441a^8b^{11}+196a^6b^{13})c^{-19}+\dots$ (25) $z_1 = 4a^4b^3c^{-7} + 10a^4b^5c^{-9} + 20a^4b^7c^{-11} + (16a^7b^6 + 35a^4b^9)c^{-13}$

 $+(64a^{11}b^6+252a^9b^8+282a^7b^{10}+84a^4b^{13})c^{-17}+...$ $z_{1} = a^{4}c^{-4} + 8a^{7}b^{3}c^{-10} + (12a^{9}b^{3} + 30a^{7}b^{5})c^{-12}$ $+(16a^{11}b^3+60a^9b^5+80a^7b^7)c^{-14}$ $+(20a^{13}b^3+100a^{11}b^5+32a^{10}b^6+200a^9b^7+175a^7b^9)c^{-16}$ $+(24a^{15}b^3+150a^{13}b^5+120a^{12}b^6+400a^{11}b^7+192a^{10}b^8$

 $+525a^9b^9+336a^7b^{11})c^{-18}+...$

 $+(36a^9b^6+84a^7b^8+56a^4b^{11})c^{-15}$